



Pre-service teachers' self-efficacy for teaching simulations and mathematical modelling with digital tools

Sebastian Gerber Prof. Dr. Hans-Stefan Siller (University of Wuerzburg)

Prof. Dr. Gilbert Greefrath

Jascha Quarder

(University of Muenster)

GEFÖRDERT VOM

Bundesministerium für Bildung und Forschung



Self-efficacy

- representation of an individual assessment of one's opportunity and ability "to organise and execute the courses of action required to produce given attainments." (Bandura 1997, S. 3)
- high self-efficacy of teachers crucial for coping with professional demands

(Kunter 2013)

- quality of teaching strongly influenced by the individual self-efficacy characteristics of the teachers
- promoting self-efficacy as a central concern of teacher education (also domain-specific self-efficacy)

(Bandura 1997)

 positive development of pre-service mathematics teachers' self-efficacy for teaching mathematical modelling by participating in specific seminars with practical activities
 (Siller et al., submitted)



Using digital tools in mathematical modelling

- facilitate the discussion of complex, authentic real-life problems (e.g. by processing a larger amount of data).
- enable other emphases (e.g. on structuring and validation) in mathematics teaching.
- can be used in all processing phases of mathematical modelling.

(Greefrath & Siller 2017)





Simulations

- are based on a previously developed mathematical model.
- serve as a digital representation of aspects of reality-related issues in the form of graphics, tables, symbolic expressions or similar forms of representation.



- support, for example, by actively changing parameters the finding of solutions in an experimental setting.
- contribute to the exploration of extra-mathematical content for which an analytical solution is not (yet) possible.

(Greefrath & Siller 2017, Podworny 2019)



Self-efficacy as an aspect of professional competence



Gerber, Quarder, Greefrath, & Siller

Baumert & Kunter (2013); Thurm & Barzel (2020, 2022); Wess et al. (2021) 5



Promoting self-efficacy

Enactive mastery experiences: promotion through experiences of success

→ By achieving realistic formulated goals, leaners recognise the value of their own abilities and skills and can use them purposefully.

Verbal persuasion: promotion through meaningful feedback

→ Learners notice their own learning progress (based on own efforts, knowledge and skills), which leads to more motivation and increasing self-efficacy.

Vicarious experience: promotion through transmission of competencies, comparison with attainments of others

Physiological and affective states: promotion through judgement of the own capabilities, strength, and vulnerability (Bandura 1997)



Research question

How does pre-service mathematics teachers' self-efficacy for teaching simulations and mathematical modelling with digital tools develop through participation in a seminar with practical school elements in comparison to pre-service mathematics teachers who do not receive a specific intervention for this domain-specific self-efficacy?



- quasi-experimental intervention study: pre-post design with two groups
- data from 146 pre-service mathematics teachers at the universities of Wuerzburg and Muenster at the beginning and end of a semester

pretest	FG	seminar with practical school elements supporting self-efficacy for teaching simulations and mathematical modelling with digital tools				
		preparation phase practical phase reflection phase	test			
	CG	other didactic courses no support for domain-specific self-efficacy	bost			



experimental group (EG): 80 pre-service mathematics teachers who took part in our seminar and thus
received specific intervention for self-efficacy for teaching simulations and mathematical modelling with
digital tools





• control group (CG): 66 pre-service mathematics teachers who participated in courses with other thematic orientations during the same period and did not receive specific intervention on this domain-specific self-efficacy

pretest	FG	seminar with practical school elements supporting self-efficacy for teaching simulations and mathematical modelling with digital tools				
	LG	preparation phase	practical phase	reflection phase	est	
	CG	no sup	other didactic courses port for domain-specific self-eff	icacy	postt	



	Number	Sex	Age		Semester		Abitur grade	
		m/f/d/n. s.	Μ	SD	Μ	SD	Μ	SD
EG	80	28/51/0/1	22.24	3.84	6.25	3.00	1.78	0.49
CG	66	28/38/0/0	23.58	3.18	8.45	3.24	1.90	0.51
Total	146	56/89/0/1	22.84	3.60	7.25	3.29	1.84	0.50

Methodical framework: test instrument

- two scales of a test instrument that captures aspects of professional competence for teaching simulations and mathematical modelling with digital tools (→ Gerber & Quarder 2022)
- scale *tasks*: six items; scale *lesson*: six items
- statement to which the personal degree of agreement is expressed via a six-point Likert scale (1 = strongly disagree; 6 = strongly agree).



Methodical framework: test instrument

Scale	ltem number	Example item	Cronbach- alpha
Task-related self-efficacy	6	I am confident that I can work out multiple ways of solving a modelling task in which digital tools are used.	.89
Lesson-related self-efficacy	6	I am confident that I can carry out teaching phases in which digital tools are used for mathematical modelling.	.90

 reliabilities (evaluated with Cronbach's alpha): high; indicate reliable results especially in group comparisons



Methodical framework: intervention

- promote self-efficacy for teaching simulations and mathematical modelling with digital tools
- intervention: one-semester seminar with practical school elements





Results: descriptive





Results: inductive

- for both dimensions *tasks* and *lessons*: regression analyses
- linear model equation: $posttest = b_0 + b_1 \cdot pretest + b_2 \cdot group$ (For group membership, the experimental group was coded with one and the control group with zero)
- necessary prerequisites for these analyses were fulfilled



Results: inductive

task-related self-efficacy:

- group membership was a significant predictor ($\beta = .21$, p < .001) for the posttest scores, with pretest scores held constant
- model specified in this way clarified 26 percent of the differences in the task-related self-efficacy at the second time of measurement ($R^2 = .26$, F(2,143) = 25.14, p < .001)

Criterion	Coefficient	b	SE	β	p
Posttest	Intercept	2.29	0.30		.000
	Pretest	0.49	0.07	. 49	.000
	Group	0.37	0.13	. 21	.005



Results: inductive

lesson-related self-efficacy:

- group membership controlling for pretest scores was found to be a significant predictor ($\beta = .28$, p < .001) for the posttest results
- the two predictors accounted for 21 percent of the differences in lesson-related self-efficacy at the second time of measurement ($R^2 = .21$, F(2,143) = 18.88, p < .001)

Criterion	Coefficient	b	SE	β	p
Posttest	Intercept	3.05	0.27		.000
	Pretest	0.33	0.06	. 41	.000
	Group	0.42	0.11	. 28	.000



Discussion

- study on the effectiveness of university seminars in promoting self-efficacy in the teaching area of simulations and mathematical modelling with digital tools
- two promotion possibilities according to Bandura (1997): enactive mastery experiences and verbal persuasion
- data collection: two measurement points (at the beginning and end of the semester) in closed response formats
- no individual qualitative investigation of the reasons for the change in self-efficacy



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Discussion

- theoretical and practical occupation with tasks and practical teaching elements within the framework of a seminar were able to promote the self-efficacy in the dimensions of *tasks* and *lesson*
- regression analysis: the data collected suggested a significant predictive power of group membership with a small practical relevance for the scores in the posttest in both dimensions





Discussion

- control croup: no *specific* support in form of our seminar, but parts of the control group may have attended other didactic courses
- outlook:
 - larger, cumulative sample
 - investigation of further aspects



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Thank you for your attention!

Sebastian Gerber Prof. Dr. Hans-Stefan Siller

(University of Wuerzburg)

sebastian.gerber@uni-wuerzburg.de

Jascha Quarder Prof. Dr. Gilbert Greefrath

(University of Muenster)

jascha.quarder@uni-muenster.de



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